Geometric Identification of Carryng Frame of Radial-axial Bearing at Hydraulic Excavators

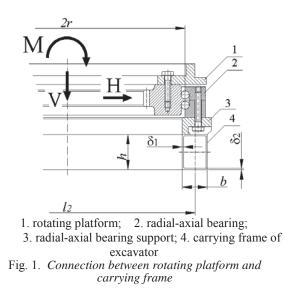
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Rotating and stationary parts of some building and transport machines (excavators, portal cranes, column cranes) are connected by radial-axial bearings of big diameters which transfer not only forces but moments as well. The paper shows the research results of relations among geometric dimensions of carrying frame elements which are important for reliable functioning of the bearings. The first part of the paper deals with theoretical analysis of the influence of relations between these geometric dimensions on rigidity of the carrying frame of excavators. The second part of the paper presents the experimental analysis of changes in rigidity relation depending on characteristic parameters of realized structures of two carrying frames of excavators. Comparative analysis of theoretical and experimental results has shown a high reliability and confirmed theoretical relations defined in the paper.

Keywords: carrying frame, excavator, rigidity, bearing, experiment

0. INTRODUCTION

Rotating platform and carrying structure of some building and transport machines, such as hydraulic excavators, rotor excavators, portal cranes, column cranes, are connected by radial-axial bearings having big diameters (Fig. 1). Manufacturers who produce these bearings [1], define the conditions regarding their lifetime and reliability. These bearings have small dimensions of cross section in comparison to diameter, i.e. their rigidity can not prevent deplanation of the plane in which bearing elements move (balls or rolls). Thus, rigidity of carrying frame has to meet some conditions for reliable transfer of forces and moments when the excavator platform rotates [2] and [3]. The paper analyses theoretical relations among geometrical dimensions of carrying frame elements which have important influence on frame rigidity. These results have been verified by laboratory measurements made on the frames of realized structures.



1. MODEL DEFINING

If relations among geometric dimensions of carrying frame of radial-axial bearing are analysed, geometric dimensions of carrying frame which provide efficient distribution of load along the circumference of the bearing can be defined [4], [5], and [6]. Loads, which are transferred from rotating platform to the carrying frame, are shown in Fig. 1. Basic geometric dimensions of cross section elements of carrying frame are also presented in Fig. 1.

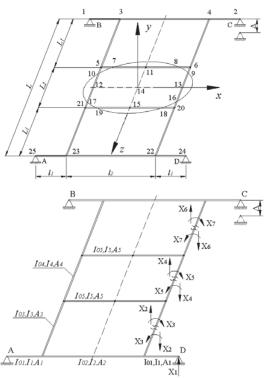


Fig. 2. Model of excavator carrying frame

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When excavator is operating there is an inclination of its carrying structure because of the lowering of a support and predistribution of vertical loads, as a result of basic elements deformations. For example, if support *C* is lowered for Δ value (Fig. 2,a), the basic system has the form presented in Fig. 2,b, where an unknown value X_i and $X_i(i=2,...,7)$ are introduced instead of support D and rejected connections, respectively.

The system of canonical equations for the system shown in Fig. 2, b is:

$$A \cdot \vec{X} = \vec{\Delta} \,. \tag{1}$$

where:

A- square matrix, consisted of influential coefficients,

 \overline{X} - vector of unknown forces and moments,

 $\vec{\Delta}$ - vector of free members.

Influential coefficients δ_{ik} (*i*=1,2,...,7; *k*=1,2,...,7) which represent the members of square matrix A, can be determined by Mohr's integral [7].

$$\delta_{ik} = \int_{l} \frac{M_{ik} \cdot M_{ii}}{G \cdot I_0} \cdot dx + \int_{l} \frac{M_{zk} \cdot M_{zi}}{G \cdot I_z} \cdot dx + \int_{l} \frac{M_{yk} \cdot M_{yi}}{G \cdot I_y} \cdot dx + \int_{l} \frac{M_{yk} \cdot M_{yi}}{G \cdot I_y} \cdot dx + \int_{l} \frac{K_k \cdot N_k}{E \cdot a} \cdot dx + \int_{l} \frac{K_z \cdot Q_{zk} \cdot Q_{zi}}{G \cdot A} \cdot dx + \int_{l} \frac{K_y \cdot Q_{yk} \cdot Q_{yi}}{G \cdot A} \cdot dx + \int_{l} \frac{K_y \cdot Q_{yk} \cdot Q_{yi}}{G \cdot A} \cdot dx$$
(2)

Since tension and shearing influences are far smaller than bending and torsion influences, the last three integrals are neglected in further analysis. Vereschagin's procedure can be used to solve expression (2). If relation between geometrical parameters of carrying frame elements is introduced the following relations can be defined (Fig. 2).

$$\begin{split} \psi &= L_1 / L_2; \quad \eta = I_5 / I_2; \quad \beta = I_4 / I_2; \quad \lambda = \delta_2 / \delta_1; \\ \varphi &= I_3 / I_2; \quad w = I_1 / I_2; \quad I_2 = I_1; \qquad k = h / b; \end{split}$$
(3)

Influential coefficients δ_{ik} are:

$$\begin{split} \delta_{11} &= \frac{4w^3 l_2^3}{3E I_2} + \frac{2w l_2^3}{E I_2} \cdot \left(1 + w + \frac{1}{3w}\right) + \frac{2\mu\psi L_2 l_2}{\varphi E I_2} + \frac{\mu L_2 l_2}{\beta E I_2}; \\ \delta_{12} &= \frac{l_2^3}{6E I_2} \left(3w + 2\right); \ \delta_{13} = -\frac{l_2^2}{2E I_2} \left(2w + 1\right) - \frac{\mu\psi L_2 l_2}{\varphi E I_2}; \\ \delta_{14} &= 0; \quad \delta_{15} = -\frac{\mu L_2 l_2}{\beta E I_2}; \quad \delta_{16} = \delta_{12}; \quad \delta_{17} = \delta_{13}; \\ \delta_{22} &= \left(1 + \frac{1}{\eta}\right) \left[\frac{l_2^3}{3E I_2} + \frac{\mu\psi^2 L_2^2 l_2}{4E I_2}\right] + \frac{\psi^3 L_2^3}{6\varphi E I_2}; \\ \delta_{23} &= -\frac{l_2^2}{2E I_2} \left(1 + \frac{1}{\eta}\right); \quad \delta_{24} = \frac{l_2^3}{3\eta E I_2} + \frac{\mu\psi L_2^3 l_2}{4\eta E I_2}; \\ \delta_{25} &= \frac{l_2^3}{2\eta E I_2}; \quad \delta_{26} = 0; \quad \delta_{27} = 0; \\ \delta_{33} &= \frac{l_2}{E I_2} \left(1 + \frac{1}{\eta}\right) + \frac{2\mu\psi L_2}{\varphi E I_2}; \quad \delta_{34} = \frac{l_2^2}{2\eta E I_2}; \end{split}$$

$$\begin{split} \delta_{35} &= -\frac{l_2}{\eta E I_2}; \quad \delta_{36} = 0; \quad \delta_{37} = 0; \\ \delta_{44} &= \frac{2l_2^3}{3\eta E I_2} + \frac{L_2^3}{6\beta E I_2} + \frac{\mu L_2^2 l_2}{2\eta E I_2}; \\ \delta_{45} &= -\frac{l_2^2}{\eta E I_2}; \quad \delta_{46} = \delta_{24}; \quad \delta_{47} = \delta_{34}; \\ \delta_{55} &= \frac{2l_2}{\eta E I_2} + \frac{2\mu L_2}{\eta E I_2}; \quad \delta_{56} = \delta_{34} = \delta_{25}; \\ \delta_{57} &= \delta_{35}; \quad \delta_{66} = \delta_{22}; \quad \delta_{67} = \delta_{23}; \quad \delta_{77} = \delta_{33}; \end{split}$$

The system of canonical equations (1) is solved by programme DELTA 3 [8]. The following coefficients are varied:

$$\begin{split} &k{=}1.0, \ 1.5, \ 2.0, \ 2.5, \ 3.0, \ 3.5; \\ &\psi = 0.0, \ 0.2, \ 0.4, \ 0.6, \ 0.8, \ 1.0; \\ &\beta = 1.0, \ 1.5, \ 2.0, \ 2.5; \\ &\delta{=}10, \ 1.5, \ 2.0, \ 2.5; \\ &\phi = 1.0, \ 1.5, \ 2.0, \ 2.5; \\ &\phi = 1.0, \ 1.5, \ 2.0, \ 2.5; \\ &\mu{,}{=}1.0, \ 1.5, \ 2.0, \ 2.5; \\ &w{=}0.4, \ 0.6, \ 0.8, \ 1.0; \end{split}$$

2. RIGIDITY OF CARRYING FRAME DEPENDING ON CHANGES OF CHARACTERISTIC PARAMETERS

If research results obtained by programme DELTA 3 are analysed, functional relations between rigidity and geometrical dimensions of carrying frame can be defined. The analysis has been made under following conditions:

a) constant geometrical dimensions:

b - width of box-like member of carrying frame,

 δ_1 , δ_2 - thicknesses of vertical and horizontal sheet of box-like members of carrying frame,

 l_2 - distance between cross members of carrying frame.

 L_2 - distance between intermediate longitudinal members of carrying frame,

 Δ - clearance at support C of carrying frame.

b) constant coefficients:

k - relation between height and width of box-like member of carrying frame,

 λ - relation between thicknesses of horizontal and vertical sheets of box-like member of carrying frame.

c) variable coefficients: $n \beta w \alpha w$ defined by relations

 η , β , w, φ , ψ - defined by relations 3.

2.1 Influence of changes in coefficient λ on rigidity of carrying frame

Fig. 3-6 shows the influences of characteristic parameters on the rigidity of carrying frame, presented by additional force at support D with defined clearance Δ . When coefficient λ is increased the rigidity of carrying frame is also increased. The change in relation between rigidities of carrying frame has the same form if λ is bigger than 1.5, so these changes in relations are not presented in the paper.

Following conclusions can be made on the basis of results presented in diagrams:

- 1. If coefficient β is increased, the rigidity of carrying frame is also increased, but the maximum coefficient of rigidity increase is $\beta = 1 \div 1.5$;
- 2. If coefficient ω is increased, the rigidity of carrying frame is decreased. The coefficient of rigidity decrease is visible for $\omega = 0.4 \div 0.6$. If $\omega = 0.8 \div I$ the change in rigidity is four times smaller than previous values.
- 3. If coefficient ψ is increased, the rigidity of carrying frame is decreased. Decrease coefficient is almost negligible for $\psi=0.8\div 1.0$.
- 4. If coefficient φ is increased, the rigidity of carrying frame is increased whereas increase coefficient is almost constant for the same value of coefficient φ .

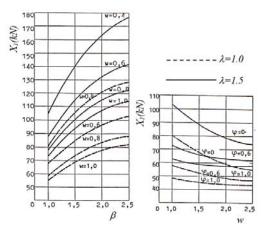


Fig. 3. The values of X_1 depending of coefficient β , $w i \phi$

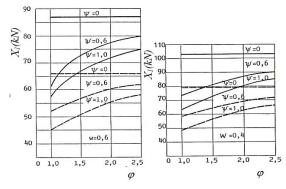


Fig. 4. The values of X_1 depending of coefficient φ i ψ

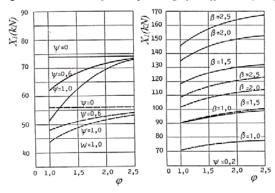


Fig. 5. The values of X_1 depending of coefficient φ , β i ψ

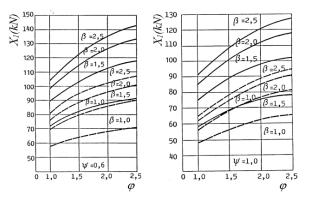


Fig. 6. The values of X_1 in function of coefficient φ , β i ψ

2.2 Influence of changes in coefficient k on rigidity of carrying frame

If results obtained by programme DELTA 3 are used, it is possible to define the relations between frame rigidities depending on changes in coefficient *k*. The research has been done for the following values of coefficient k=1.0;2.0;3.0, for different geometric characteristics of members L_2 and l_2 , and for different coefficients ψ and w. Tables 1,2,3,4,5 and 6 show the values of forces at support *D* with constant clearance at support *C* for w=0,5 and w=1,0.

Table 1. The values of X_{kl} forces

			1	w=0.5		
	L_2	l_2	ψ	X_{kl}	C_{k2}/C_{k1}	$\left(k_2/k_1\right)^{\sqrt{3}}$
	1000	1000	0.5	57.16	3.34	
	1000	1000	1.0	46.75	3.10	
$k_1 = 1$	2000	2000	0.5	7.09	3.34	3.32
$\kappa_I = I$	2000	2000	1.0	5.79	3.10	3.32
	5000	5000	0.5	0.45	3.35	
	5000	5000	1.0	0.37	3.10	

Table 2. The values of X_{k2} forces

			١	w=0.5		
	L_2	l_2	Ψ	X_{k2}	C_{k3}/C_{k2}	$\left(k_3 / k_2\right)^{\sqrt{3}}$
	1000	1000	0.5	191.37	2.02	
	1000	1000	1.0	144.67	1.95	
$k_{2}=2$	2000	2000	0.5	23.70	2.02	2.02
K2=2	2000	2000	1.0	17.91	1.95	2.02
	5000	5000	0.5	1.51	2.02	
	5000	5000	1.0	1.14	1.95	

Table 3. The values of X_{k3} forces

			1	w=0.5		
	L_2	l_2	Ψ	X_{k3}	C_{k3}/C_{k1}	$\left(k_3 / k_1\right)^{\sqrt{3}}$
	1000	1000	0.5	386.45	6.76	
	1000	1000	1.0	281.90	6.03	
$k_3=3$	2000	2000	0.5	47.85	6.75	6.7
K3=3	2000	2000	1.0	34.89	6.03	
	5000	5000	0.5	3.05	6.77	
	5000	5000	1.0	2.22	6.00	

The values shown in tables 1, 2 and 3 are related to: w = 0, 5

- b = 300 mm width of box-like member of carrying frame;
- $\delta_1 = 10 \, mm$ thickness of vertical sheet of box-like member of carrying frame;
- $\Delta = 5 mm$ clearance at support C.

The values shown in tables 4, 5, and 6 are related to:

w = 1,0

- $b = 300 \, mm$ width of box-like member of carrying frame;
- $\delta_1 = 10 \, mm$ thickness of vertical sheet of box-like member of carrying frame;

 $\Delta = 5 mm$ - clearance at support C.

Table 4. *The values of* X_{kl} *forces*

				w=1		
	L_2	l_2	Ψ	X_{kl}	C_{k2}/C_{k1}	$\left(k_2 / k_1\right)^{\sqrt{3}}$
	1000	1000	0.5	49.72	3.60	
	1000	1000	1.0	43.94	3.23	
$k_l = l$	2000	2000	0.5	6.15	3.60	3.32
$\kappa_1 = 1$	2000	2000	1.0	5.43	3.23	
	5000	5000	0.5	0.39	3.61	
	5000	5000	1.0	0.35	3.20	

Table 5. The values of X_{k2} forces

				w=1		
	L_2	l_2	Ψ	X_{k2}	C_{k3}/C_{k2}	$\left(k_3 / k_2\right)^{\sqrt{3}}$
	1000	1000	0.5	179.23	2.07	
	1000	1000	1.0	142.19	1.97	
$k_2=2$	2000	2000	0.5	22.16	2.07	2.02
$\kappa_2 = 2$	2000	2000	1.0	17.57	1.97	
	5000	5000	0.5	1.41	2.07	
	5000	5000	1.0	1.12	1.96	

Table 6. The values of X_{k3} forces

				w=1		
	L_2	l_2	ψ	X_{k3}	C_{k3}/C_{k1}	$\left(k_3 / k_1\right)^{\sqrt{3}}$
	1000	1000	0.5	372.06	7.48	
	1000	1000	1.0	280.85	6.38	
$k_3=3$	2000	2000	0.5	46.00	7.48	6.7
кз=5	2000	2000	1.0	34.66	6.38	
	5000	5000	0.5	2.93	7.51	
	5000	5000	1.0	2.20	6.28	

If relation between coefficients k is increased, then relation between rigidities of carrying frame is also increased according to the following relation:

$$\frac{C_{ki}}{C_{kj}} = \left(\frac{k_i}{k_j}\right)^{\sqrt{3}} \tag{4}$$

Fig. 4 shows relations C_{k2}/C_{k1} , C_{k3}/C_{k1} , and C_{k3}/C_{k2} , for coefficients $\psi=0.5$ and $\psi=1.0$; w=0.5 and w=1.0; b=const; $\Delta=const$; $\delta_1=const$; $L_2/l_2=1000,2000$ i 5000 mm. Relation $(k_i/k_i)^{\sqrt{3}}$ is presented, too.

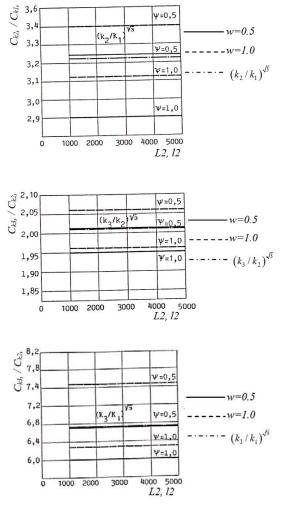


Fig. 7. Diagrams of changes in rigidity of carrying frame depending on coefficient k

2.3 Influence of changes in geometrical values L and l on rigidity of carrying frame

Relation of changes in rigidity of carrying frame can be defined depending on changes in geometrical values of L and l for different parameters of ψ abd w. Tables 7 and 8 show the force values at support D, for constant clearance at support C for values w=0,5 and $w=1,0; \ \delta=10 \ mm; \ k=1,0; \ \lambda=1,0; \ b=300 \ mm;$ and for w=0,4 i $w=0,7; \ \delta=10 \ mm; \ k=3,0; \ \lambda=1,5; \ b=300 \ mm.$

Table 7. *The force values at support D;* Δ =*const,* w=0.5;1 *i* ψ =0;0,5;1

		w=0.5			w=1.0	
l_2, L_2	$\psi=0$	$\psi = 0.5$	$\psi = 1$	$\psi=0$	$\psi = 0.5$	$\psi = 1$
1000, 1000	72.46	57.16	46.75	54.85	49.72	43.94
2000, 2000	8.99	7.09	5.79	6.79	6.15	5.43
3000, 3000	2.66	2.09	1.72	2.01	1.83	1.61
4000, 4000	1.1	0.88	0.72	0.85	0.77	0.68
5000, 5000	0.57	0.45	0.37	0.43	0.39	0.35

Table 8. <i>The force values at support D</i> ; $\Delta = const, w = 0.4; 0.7$
i ψ=0;0,5;1

		w=0.4		w=0.7			
l_2, L_2	$\psi=0$	$\psi = 0.5$	$\psi = 1$	$\psi=0$	$\psi = 0.5$	$\psi = 1$	
1000, 1000	713.98	435.85	311.32	629.83	412.85	302.03	
2000, 2000	88.47	53.96	38.54	78.02	51.10	37.38	
3000, 3000	26.14	15.94	11.38	23.05	15.09	11.04	
4000, 4000	11.01	6.71	4.79	9.71	6.35	4.65	
5000, 5000	5.63	3.43	2.45	4.96	3.25	2.38	

Tables 9 and 10 show that the increase of distance *L* for constant values of *w*, δ , k, λ and *b* causes the decrease of relation between rigidities of carrying frames according to following relation:

$$\left(C_{Li} / C_{Lj}\right) = \left(L_j / L_i\right)^3.$$
⁽⁵⁾

Relations (C_{Li}/C_{Lj}) depending on coefficients φ , ψ , w, k and λ , for constant values of b, δ_l and Δ are presented in tables 9 and 10. Values of $(L_j/L_i)^3$ are shown, too.

Table 9. The relations (C_{Li}/C_{Lj}) depending on coefficient φ , ψ , w, k=1 i $\lambda=1$; b=const, $\delta_1=const$ and $\Delta=const$

$k=1.0; \lambda=1.0;$							
G (G		w=0.5		,	w=1.0		$\left(L_j/L_i\right)^3$
$C_{\rm Li}/C_{\rm Lj}$	$\psi=0$	ψ=0.5	ψ=1	$\psi=0$	ψ=0.5	ψ=1	
$C_{\rm L1}/C_{\rm L2}$	8.06	8.06	8.07	8.07	8.08	8.09	8
$C_{\rm L1}/C_{\rm L3}$	27.24	27.34	27.18	27.28	27.16	27.29	27
$C_{\rm L1}/C_{\rm L4}$	65.28	64.95	64.93	64.53	64.57	64.61	64
$C_{\rm L1}/C_{\rm L5}$	127.12	127.02	126.35	127.55	127.48	125.54	125
$C_{\rm L2}/C_{\rm L3}$	3.37	3.39	3.36	3.37	3.36	3.37	3.375
$C_{\rm L2}/C_{\rm L4}$	8.09	8.05	8.04	7.99	7.99	7.98	8
C_{L2}/C_{L5}	15.77	15.75	15.65	15.79	15.77	15.51	15.625
C_{L3}/C_{L4}	2.39	2.37	2.38	2.36	2.37	2.36	2.37
C_{L3}/C_{L5}	4.66	4.64	4.65	4.67	4.69	4.60	4.629
C14/C15	1.95	1.95	1.94	1.97	1.97	1.94	1.953

Table 10. *The relations* (C_{Li}/C_{Lj}) *depending on coefficient* φ , ψ , w, k=3 *i* $\lambda=1.5$; b=const, $\delta_1=const$ and $\Delta=const$

	$k=3.0; \lambda=1.5;$							
a (a	W=0.4			1	$\left(L_{j}/L_{i}\right)^{3}$			
C _{Li} /C _{Lj}	ψ=0	ψ=0.5	ψ=1	ψ=0	ψ=0.5	ψ=1	() .)	
$C_{\rm L1}/C_{\rm L2}$	8.07	8.07	8.08	8.07	8.08	8.09	8	
$C_{\rm L1}/C_{\rm L3}$	27.31	27.34	27.35	27.32	27.36	27.35	27	
$C_{\rm L1}/C_{\rm L4}$	64.85	64.95	64.99	64.86	65.01	64.95	64	
$C_{\rm L1}/C_{\rm L5}$	126.81	127.07	127.07	126.98	127.03	126.90	125	
$C_{\rm L2}/C_{\rm L3}$	3.38	3.38	3.38	3.38	3.38	3.38	3.375	
$C_{\rm L2}/C_{\rm L4}$	8.03	8.04	8.04	8.03	8.05	8.04	8	
$C_{\rm L2}/C_{\rm L5}$	15.71	15.73	15.73	15.73	15.72	15.70	15.625	
$C_{\rm L3}/C_{\rm L4}$	2.37	2.37	2.37	2.37	2.38	2.37	2.37	
$C_{\rm L3}/C_{\rm L5}$	4.64	4.64	4.65	4.65	4.64	4.64	4.629	
$C_{\rm L4}/C_{\rm L5}$	1.95	1.96	1.95	1.96	1.95	1.95	1.953	

3. EXPERIMENT AND RESULTS

Experimental verification has been made in order to verify theoretical results which are related to the rigidity of carrying frame. The experiment has been made on two carrying frames of excavators, types BGH 600 and BGH 10000, made by IMK 14. oktobar, Serbia [9]. The carrying frames are supported by steel spheres, sets of sheet metal of various thicknesses, force transducers, basic plates lying on reinforced concrete basis. One of supports is shown in Fig. 8. Sheet metal sets consist of various thicknesses of plates so that clearance Δ between frame supports and steel spheres can be achieved by drawing some plates.

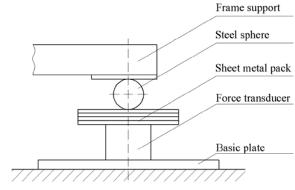


Fig. 8. One of frame supports

Instrumentation and measuring points are shown in Figs.7, 8 and 9, respectively.

The experiment has been made when carrying frame is supported by supports and when one of them is lowered for value Δ in comparison to other supports. The frame is loaded by the weight of rotating platform along with operating equipment and additional load [11]. Rotation has been made in each 45°.

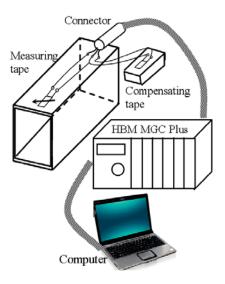


Fig. 9. Layout of connection between measuring devices[10]

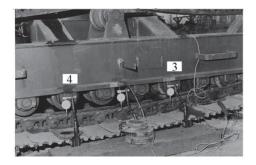


Fig. 10. Measurement of displacements of characteristic points of carrying frame

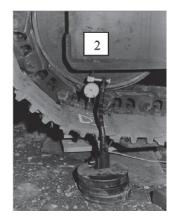


Fig. 11. Point 2 of measurement of displacements

A series of results have been obtained in the experiment in conformity with defined programme. The paper shows the results which are significant for experimental verification of theoretical model. Thus, comparative results are obtained for displacements of characteristic points (Fig. 2b) of carrying frames, types BGH 600 and BGH 100, made by IMK 14.oktobar, Serbia. For distances L=2250 mm (BGH 600) and L=2410 mm (BGH 1000) displacements of characteristic points are shown in table 11.

Displacements f_I and f_{II} at support 2 are important for further analysis of experimental results.

If relation (5) is applied:

$$\left(\frac{L_{II}}{L_{I}}\right)^{3} = \frac{C_{I}}{C_{II}} = \frac{f_{II}}{f_{I}}$$
$$\left(\frac{2410}{2250}\right)^{3} = \frac{-2.91}{-2.40}$$
$$1.23 \approx 1.21$$

Theoretical relation (4) and measurement results show high compatibility. The following relations are based on geometrical characteristics of carrying frame:

$$\left(\frac{k_I}{k_{II}}\right)^{\sqrt{3}} = \frac{C_{kI}}{C_{kII}} = \frac{f_{II}}{f_I}$$
$$\left(\frac{0.857}{0.767}\right)^{\sqrt{3}} = \frac{-2.91}{-2.40}$$
$$1.21 = 1.21$$

Table 11. Displacements	of characteristic points of
carryng frame	

yng jrame		
	BGH 600;	BGH 1000;
Characteristic	L _I =2250 mm;	L _{II} =2410 mm;
points	Displacements	Displacements f _{II}
	$f_{I}(mm)$	(mm)
2	-2.40	-2.91
3	-0.94	-1.12
4	-1.69	-1.90
5	-0.69	-0.78
6	-1.29	-1.38
7	-0.51	-0.60
8	-0.97	-1.07
9	-0.61	-0.74
10	-0.33	-0.42
11	-0.1	-0.15
12	-0.05	-0.10

Therefore, theoretical relation (4) is proved, too. The obtained relations can be of great importance for continuation of research taking into account the stiffening ring whose calculation can be performed by using the methodology [12-14] and optimization of mentioned parameters [15].

4. CONCLUSION

Theoretical and experimental results clearly define the influence of relation between geometrical dimensions of characteristic parameters of carrying frame on its rigidity. Out of large number of obtained results only the results which are significant for defining the frame rigidity are stated:

- if relation between height and width of members of boxlike cross sections, the relation between rigidities of these members are also increased. The increase of rigidity relation is defined by relation between coefficients k raised to a power $\sqrt{3}$,
- if distance between longitudinal axes of carrying frame is increased, the relation between rigidities is decreased. Decrease relation between frame rigidities is inversely proportional to cubic relation of distance between longitudinal axes of carrying frame.

These results provide forming the excavator carrying frames enabling necessary rigidity of basic surface on which radial-axial bearing is supported. The results are also important for stress analysis of the carrying frames and for defining the stress dissipation in the frame elements.

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