

High bandwidth performance of multimode graded-index microstructured polymer optical fibers

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ABSTRACT

The investigation of the bandwidth in multimode graded-index microstructured polymer optical fiber (GI mPOF) with a solid core is proposed using a modal diffusion approach. For a variety of launch radial offsets of multimode GI mPOF, bandwidth is reported by numerically solving the time-dependent power flow equation (TD PFE) using the explicit finite difference method (EFDM) and physics-informed neural networks (PINN). The decline in bandwidth with fiber length becomes slower at fiber lengths close to the coupling length L_c at which an equilibrium mode distribution (EMD) is attained, showing that mode coupling enhances bandwidth at longer fiber lengths. As fiber length is increased, bandwidth approaches complete independence from radial offset, suggesting the steady-state distribution (SSD) has been reached. We compare multimode GI mPOF performance in terms of bandwidth with that of traditional multimode GI POFs made of the same material. Higher bandwidth performance and quicker bandwidth improvement are displayed by the GI mPOF. To enhance fiber performance in GI mPOF links, such a fiber characterization can be used.

Introduction

High-speed short-range signal transmission via POF has drawn a lot more attention in recent years [1–2]. POF's benefits of a large core, a simple connection, and a diversity of materials [3–16] may offer a cost-effective option for the in-home network. Up until now, POF has most typically been produced using Polymethyl-methacrylate (PMMA) [17]. POF can generally be divided into three types: single-mode [18], few-mode [12], and multimode [19] fibers. The two refractive index (RI) distributions that are most frequently used to create POFs are step-index (SI) [20] and GI [21] distributions. The RI distribution of GI multimode POF continually lowers from the core axis to the cladding. Using this RI distribution, intermodal dispersion can be reduced, the POF's bandwidth can be improved, and transmission distance may be raised. However, in order to manufacture GI POF, advanced doping techniques are required.

The versatility in designing the optical fiber is greatly increased by the microstructure of microstructured optical fiber (MOFs). Many

excellent MOF properties [22], including birefringence [23], light dispersion [24], supercontinuum light [25], and wavelength conversion [26], have been investigated by modifying the microstructure. The fabrication of multimode mPOF was first reported by Eijkelenborg et al. in 2001 [27], and afterwards, mPOF garnered research interest for its various uses [28–29]. An optical fiber called a multimode mPOF is made to simultaneously guide numerous light modes. It has a core region surrounded by cladding, and the core and/or cladding region's periodic arrays of air holes give it its distinctive structure. Thus, an mPOF can have its core and/or cladding layer modified by changing the placement and/or size (d) of air holes (Fig. 1). In Fig. 1, a mPOF that mimics a GI optical fiber features a core with different-sized air-holes. Instead of requiring complex doping methods, GI mPOF has the advantage of being more adjustable when it comes to altering the air-hole diameters d and pitch Λ . Additionally, research has shown that GI mPOF has a wider bandwidth than conventional multimode GI POF [30,31]. Numerous industries, including telecommunications, sensing, and imaging in medicine, use multimode GI and SI mPOFs. They are appropriate for

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high-power applications due to their large mode areas and ability to transmit high-power lasers. Due to their high sensitivity to variations in the refractive index of the surrounding medium, they are also beneficial for sensing applications.

The PFE is used to characterize transmission performance of different types of conventional multimode optical fibers [31–35] and is thus the most promising tool for modeling multimode MOFs. Since other two alternative approaches, wave optics or geometrical optics, are not able to offer an efficient and accurate modeling tool for transmission characteristics of multimode optical fibers (including MOFs), the importance of the approach used in this work is obvious. A very good efficiency and accuracy of the method used in this work has already been demonstrated in modeling bandwidth of conventional multimode GI POF [35]. Following this route, the bandwidth in GI mPOF for a various launch radial offsets is determined in this paper, to the best of our knowledge for the first time, by numerically solving the TD PFE. These theoretically obtained results for multimode GI mPOF bandwidth are contrasted with previously reported bandwidth for conventional multimode GI POFs [35]. The results reported in this study can be useful for various MOFs applications [36–39].

GI mPOF design

Fig. 1 shows a GI mPOF that was considered in this investigation. Six air-hole rings, numbered rings 1, 2, ..., 6, make up the GI mPOF. The fiber material is a PMMA, and the air holes are held in place by a triangular lattice with a pitch of Λ . The air-hole diameter in rings 5 and 6 is the same as the air-hole diameter in ring 4 ($d_4 = d_5 = d_6$). The TD PFE was used to simulate this system.

TD PFE for GI optical fibers

The RI profile of GI optical fiber may be expressed as:

$$n(r, \lambda) = \begin{cases} n_{co}(\lambda) \left[1 - 2\Delta(\lambda) \left(\frac{r}{a} \right)^g \right]^{1/2} & (0 \leq r \leq a) \\ n_{cl}(\lambda) [1 - 2\Delta(\lambda)]^{1/2} = n_{cl}(\lambda) & (r > a) \end{cases} \quad (1)$$

where $n_{co}(\lambda)$ is the maximum RI of the core (measured at the fiber axis), $n_{cl}(\lambda)$ is the RI of the cladding, $\Delta(\lambda) = (n_{co}(\lambda) - n_{cl}(\lambda)) / n_{co}(\lambda)$ is the relative RI difference, g is the core index exponent and a is the core radius (Fig. 1). The wavelength λ of the source determines the optimum value of the core RI exponent g to get the maximum bandwidth.

For multimode GI optical fibers, the TD PFE is:

$$\begin{aligned} \frac{\partial P(m, \lambda, z, \omega)}{\partial z} + j\omega\tau(m, \lambda)P(m, \lambda, z, \omega) &= -\alpha(m, \lambda)P(m, \lambda, z, \omega) + \\ + \frac{\partial P(m, \lambda, z, \omega)}{\partial m} \frac{\partial d(m, \lambda)}{\partial m} + d(m, \lambda) \frac{1}{m} \frac{\partial P(m, \lambda, z, \omega)}{\partial m} &+ d(m, \lambda) \frac{\partial P^2(m, \lambda, z, \omega)}{\partial m^2} \end{aligned} \quad (2)$$

where $P(m, \lambda, z, \omega)$ is the power in the m -th principal mode (modal group) [32], z is position along the fiber axis from the input fiber end, $\alpha(m, \lambda)$ is the attenuation coefficient, $d(m, \lambda) \equiv D$ is the coupling

coefficient, $\omega = 2\pi f$ is the baseband angular frequency, $\tau(m, \lambda)$ is delay time per unit length, which can be determined as:

$$\begin{aligned} \tau(m, \lambda) \cong \frac{n_1(\lambda)}{c} \left[1 + \frac{g-2}{g+2} \Delta(\lambda) \left(\frac{m}{M(\lambda)} \right)^{2g/(g+2)} \right. \\ \left. + \frac{1}{2} \frac{3g-2}{g+2} \Delta(\lambda)^2 \left(\frac{m}{M(\lambda)} \right)^{4g/(g+2)} \right] \end{aligned} \quad (3)$$

where c is the free-space velocity of light and:

$$P(m, \lambda, z, \omega) = \int_{-\infty}^{+\infty} P(m, \lambda, z, t) \exp(-j\omega t) dt \quad (4)$$

The maximum principal mode number is [32]:

$$M(\lambda) = \sqrt{\frac{g\Delta(\lambda)}{g+2}} a k n_1(\lambda) \quad (5)$$

where $k = 2\pi/\lambda$. Gaussian launch-beam distribution $P_0(\theta, \lambda, z=0)$ can be transformed into $P_0(m, \lambda, z=0)$ (one needs $P_0(m, \lambda, z=0)$ to numerically solve the TD PFE (2)), using the following relationship [32–34]:

$$\frac{m}{M} = \left[\left(\frac{\Delta r}{a} \right)^g + \frac{\theta^2}{2\Delta} \right]^{(g+2)/2g} \quad (6)$$

where Δr represents the radial separation (radial offset) between the launch beam point and the core center and θ represents the tilt angle measured in relation to the fiber axis. One should note that the condition of validity of the model proposed in this work is that guiding modes can be treated as a modal continuum. This is the case with all types of multimode optical fibers, such as a GI mPOF investigated in this work. Details regarding numerical solving the TD PFE (2) using EFDM and calculating bandwidth, can be found in our earlier work [35]. In this work, in order to further validate our proposed method for calculating bandwidth in a multimode GI mPOF, in our best knowledge for the first time, the TD PFE (2) is also solved using PINN. Methodology regarding numerical solving the partial differential equations (PDEs), such as TD PFE (2), using PINN are given in the Appendix A of this work.

We investigated the bandwidth in a multimode GI mPOF, which consists of different SI distributed layers (Fig. 1(b)), for which the effective V parameter is given as:

$$V = \frac{2\pi}{\lambda} a_{eff} \sqrt{n_{co}^2 - n_{fsm}^2} \quad (7)$$

where $a_{eff} = \Lambda/\sqrt{3}$ [40], and n_{fsm} is effective RI of different core and cladding layers, which can be obtained from equation (7), with the effective V parameter [40]:

$$V \left(\frac{\lambda}{\Lambda}, \frac{d}{\Lambda} \right) = A_1 + \frac{A_2}{1 + A_3 \exp(A_4 \lambda / \Lambda)} \quad (8)$$

with the fitting parameters A_i ($i = 1$ to 4) given as:

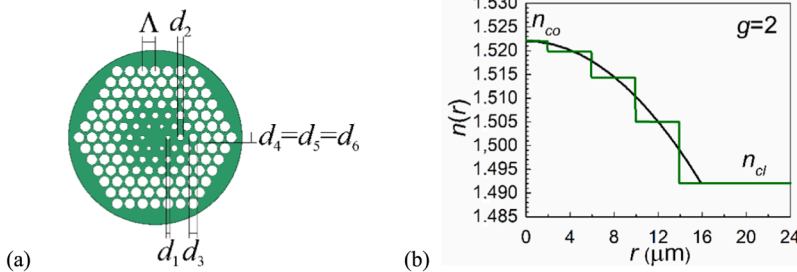


Fig. 1. (a) The cross-section of the multimode GI mPOF (PMMA is the fiber material, shown in green color). A triangular lattice's air holes are positioned using pitch Λ . The air-hole sizes of the four inner air-hole rings in the core are d_1 , d_2 , d_3 , and d_4 . The cladding's air holes in rings 5 and 6 have the same diameter as those in air-hole ring 4 ($d_4 = d_5 = d_6$). (b) The referent multimode GI mPOF's RI performance (green solid line). The parabolic distribution of the RI in the core has $g = 2$ (black solid line). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

$$A_i = a_{i0} + a_{i1} \left(\frac{d}{\Lambda}\right)^{b_{i1}} + a_{i2} \left(\frac{d}{\Lambda}\right)^{b_{i2}} + a_{i3} \left(\frac{d}{\Lambda}\right)^{b_{i3}} \quad (9)$$

where the coefficients a_{i0} to a_{i3} and b_{i1} to b_{i3} ($i = 1$ to 4) are given in Table 1.

We applied our method to the multimode GI mPOF which has a core radius $a = 4\Lambda = 16 \mu\text{m}$, where $\Lambda = 4 \mu\text{m}$, and fiber diameter $b = 1 \text{ mm}$. The GI mPOF material is PMMA, the same material as used for the GI POF (OM Giga, Fiber Fin™), which we previously investigated experimentally [35]. The RI of the core measured at the fiber axis is $n_{co} = 1.5220$ while the RI of the cladding is $n_{cl} = 1.4920$ [33,35,41]. For the GI mPOF under examination, the maximum principal mode number is $M = 24$ (the maximum mode number is $N = 580$) at $\lambda = 633 \text{ nm}$, for $g = 2.0$ and $\Delta = (n_1 - n_2)/n_1 = 0.019711$. The modal attenuation is $\alpha(m, \lambda) \equiv \alpha_c = 0.0122 \text{ m}^{-1}$ and coupling coefficient is $D = 1482 \text{ m}^{-1}$ [35] (typical values of α_c and D for conventional multimode GI POFs and multimode GI mPOFs). The similar presumption was used to model a silica MOF [42]. For $\Lambda = 4 \mu\text{m}$ and air-hole diameters of the four air-hole rings in the core $d_1 = 0.6 \mu\text{m}$, $d_2 = 0.7 \mu\text{m}$, $d_3 = 1.3 \mu\text{m}$ and $d_4 = 3.1 \mu\text{m}$, the RI $n_1 = 1.5201$, $n_2 = 1.5145$, $n_3 = 1.5050$ and $n_4 = 1.4920$, respectively, are calculated by means of equations (7) and (8). Thus, a parabolic RI distribution in the core with $g = 2.0$ is achieved (Fig. 1). The diameter of the cladding's air-holes in the rings 5 and 6 is $d_4 = d_5 = d_6 = 3.1 \mu\text{m}$, which corresponds to the cladding RI $n_4 = n_5 = n_6 = n_{cl} = 1.4920$.

A Gaussian beam is assumed to be launched with $\langle \theta \rangle = 0^\circ$ in the numerical calculations. Fig. 2 shows the numerically estimated bandwidth using EFDM and PINN for four radial offsets $\Delta r = 0, 4, 8$ and $12 \mu\text{m}$ for varied fiber lengths. A good agreement between solutions obtained using EFDM and PINN solutions can be seen. According to Fig. 2, bandwidth decreases as radial offset increases as a result of increased modal dispersion brought on by the excitation of higher guided modes. A more pronounced decline is seen with shorter fiber lengths. When the fiber length is $z \approx 20 \text{ m}$, which is close to the theoretically determined coupling length $L_c = 18 \text{ m}$ [37] at which an EMD is established, strong mode coupling results in bandwidth improvement (slower bandwidth drop) in multimode GI mPOFs. An SSD is established as fiber length increases (in our earlier work [41], we found that an SSD is established at $z = 60 \text{ m}$). As fiber length further increases, bandwidth becomes essentially radially offset-independent. Consequently, assuming a radial offset of $\Delta r = 0 \mu\text{m}$ for the examined GI mPOF, we obtain a bandwidth of around 28 GHz at a distance of 100 m, which results in a bandwidth-length product of 2.8 GHz·km. This bandwidth-length product is substantially higher than those for standard GI POFs studied in our earlier work [35] (Fig. 3) and Chun-Yu Lin et al.'s work [43], which were 0.46 GHz·km and 0.156 GHz·km, respectively. Because the GI mPOF investigated in this work has a smaller core radius and fewer propagating modes than a conventional GI POF, the EMD is obtained in GI mPOF at a shorter length. Namely, the coupling length of $L_c = 31 \text{ m}$ is reported for conventional GI POF [33]. When there are fewer propagating modes, the mode coupling process requires a shorter length to complete, accelerating the transition to the slower bandwidth drop phase. The mode coupling process requires a shorter length to complete the mode coupling process when there are fewer propagating

Table 1

The fitting coefficients in equation (9).

	$i = 1$	$i = 2$	$i = 3$	$i = 4$
a_{i0}	0.54808	0.71041	0.16904	-1.52736
a_{i1}	5.00401	9.73491	1.85765	1.06745
a_{i2}	-10.43248	47.41496	18.96849	1.93229
a_{i3}	8.22992	-437.50962	-42.4318	3.89
b_{i1}	5	1.8	1.7	-0.84
b_{i2}	7	7.32	10	1.02
b_{i3}	9	22.8	14	13.4

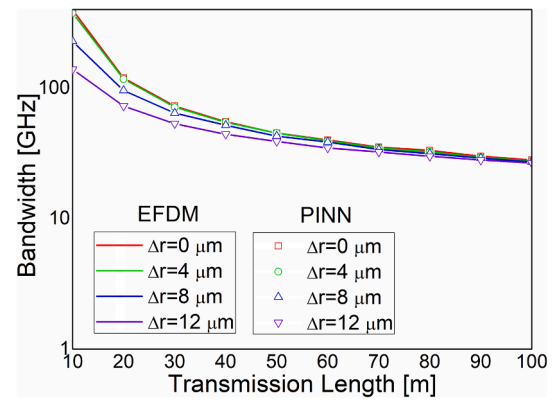


Fig. 2. Numerically calculated bandwidth using EFDM (lines) and PINN (open symbols) as a function of transmission length of GI mPOF for various radial offsets.

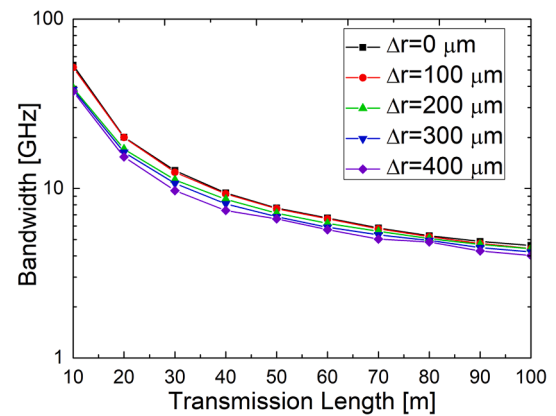


Fig. 3. Measured bandwidth (solid symbols) as a function of transmission length of conventional multimode GI POF for various radial offsets (lines are drawn to guide the eye) [35].

modes, which accelerates the transition to the slower bandwidth decline regime.

Improved fiber performance on GI mPOF lines, especially in in-home networks, can be attained by using such a fiber characterization. This optimization can be carried out by comparing the performance characteristics and numerical simulation results of different GI mPOFs with different RI distribution (different g), coupling coefficient D , and attenuation α_c . Finally, since in contrast to GI POF, fabrication of GI mPOF does not require an advanced doping techniques and, as shown in this work, and it can achieve a much higher bandwidth, it deserves recommendation as a good choice for various high bandwidth fiber optic systems. A range of different fabrication methods is available for mPOF preform fabrication, including extrusion, drilling, casting or injection molding [7,44].

Conclusion

By numerically solving the TD PFE using the EFDM and PINN, we were able to determine the bandwidth for various multimode GI mPOF launch conditions (radial offsets). We discovered that when radial offset increases, bandwidth decreases. There is a more noticeable bandwidth decrease at short fiber lengths. The fact that this decline slows down as coupling length L_c gets closer to the point at which an EMD is reached, shows how strongly mode coupling affects the bandwidth in GI mPOFs. The length at which EMD is reached is shorter, the quicker the bandwidth would change from a steep to a moderate bandwidth decrease. The formation of an SSD is indicated by the bandwidth becoming almost

entirely independent of radial offset as fiber length is extended. Consequently, for the GI mPOF that was the subject of this work, with radial offset of $\Delta r = 0 \mu m$, we obtain a bandwidth-length product of 2.8 GHz·km. This bandwidth-length product is substantially higher than those for typical GI POFs studied in our previous work [35] and Chun-Yu Lin et al.'s work [43], which were 0.46 GHz·km and 0.156 GHz·km, respectively. We have demonstrated that GI mPOF has a wider bandwidth compared to its conventional counterpart due to carefully tuned structure of the GI mPOF, which allowed reduction of modal dispersion-induced pulse spreading. Furthermore, mPOFs with a relatively large core diameter can support multiple modes, which can be used for mode-division multiplexing to increase the bandwidth.

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Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

Data will be made available on request.

Appendix A. : PINN for solving PDEs

The PINN is a machine-learning technique that can be used to approximate the solution of PDEs. PDEs with corresponding initial and boundary conditions can be expressed in a general form as [45]:

$$\begin{aligned} \frac{\partial u(x,t)}{\partial t} + N[u(x,t)] &= 0, \quad x \in \Omega, \quad t \in [0, T] \\ u(x, t=0) &= h(x), \quad x \in \Omega \\ u(x, t) &= g(x, t), \quad x \in \Omega_g, \quad t \in [0, T] \end{aligned} \quad (A1)$$

Here, N is a differential operator, $x \in \Omega \subseteq R^d$ and $t \in R$ represent spatial and temporal dimensions respectively, $\Omega \subseteq R^d$ is a computational domain, $\Omega_g \subseteq \Omega$ is a computational domain of the exposed boundary conditions, $u(x, t)$ is the solution of the PDEs with initial condition $h(x)$ and boundary conditions $g(x, t)$.

PINN consists of two subnets: an approximator network and a residual network. The approximator network receives input $u(x, t)$ undergoes the training process, and provides an approximate solution $\hat{u}(x, t)$ as an output. The approximator network trains on a grid of points, called collocation points, sampled randomly or regularly from the simulation domain. The weights and biases of the approximator network make up a set of trainable parameters, trained by minimizing a composite loss function of the following form:

$$L = L_r + L_0 + L_b \quad (A2)$$

where:

$$\begin{aligned} L_r &= \frac{1}{N_r} \sum_{i=1}^{N_r} |u(x^i, t^i) + N[u(x^i, t^i)]|^2 \\ L_0 &= \frac{1}{N_0} \sum_{i=1}^{N_0} |u(x^i, t^i) - h^i|^2 \\ L_b &= \frac{1}{N_b} \sum_{i=1}^{N_b} |u(x^i, t^i) - g^i|^2 \end{aligned} \quad (A3)$$

Here, L_r , L_0 , and L_b represent residuals of governing equations, initial and boundary conditions, respectively. N_r , N_0 , and N_b are the numbers of mentioned collocation points of the computational domain, initial and boundary conditions, respectively. These residuals are computed by a non-trainable part of the PINN model called the residual network. The approximator network is used to approximate the solution $u(x, t)$ which then goes to the residual network to calculate the residual loss L_r , boundary condition loss L_b , and initial condition loss L_0 . The weights and biases of the approximator network are trained using a composite loss function consisting of residuals L_r , L_0 , and L_b through gradient-descent technique based on the back-propagation [45]. To calculate the residual L_r , PINN requires derivatives of the outputs with respect to the inputs x and t . Such calculation is done through automated differentiation, which relies on the fact that combining derivatives of the constituent operations by the chain rule produces the derivative of the entire composition.

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