

## KINEMATIC ANALYSIS OF THE COMPLEX PLANETARY GEAR TRAIN OVERVIEW

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### 1. Introduction

Planetary gear trains represent a special type of gear transmission whose element motion resembles the movement of planets around the Sun. Thanks to their compact design and the ability to achieve high transmission ratios with a relatively low total mass, they have found application in various fields of mechanical engineering.

The basic planetary gear train (PGT) consists of two central gears (one with external teeth and the other with internal teeth), planet gears, and a carrier on which the planets are mounted. By connecting the appropriate elements to the input and output shafts, as well as by fixing certain components, different configurations or planetary gear train schemes can be obtained. This is described in the literature [1] and [2]. By adding gears and carriers to the structure of a simple planetary gear train, complex planetary gear trains are formed. Their advantage over simple ones lies in achieving a greater number of different transmission ratios. This has defined the wide application of PGT in automatic transmissions of various passenger and heavy-duty vehicles, as well as buses and construction machinery.

To determine the transmission ratios, or the speeds of a multi-stage planetary gear train, it is necessary to understand the kinematics of the coupling between its elements. Considering the complexity of the motion, this represents a very challenging task. In books [1, 2], the most commonly used methods for solving the kinematics of PGT are presented.

The applying of these methods for determining the transmission ratios of a complex PGT requires a great deal of time due to the increasing complexity of the motion equations and the difficulty in expressing the transmission ratios caused by the large number of degrees of freedom. Because of these shortcomings, an overview of research related to new methods for determining the speeds of the complex Ravigneaux planetary gear train (RPGT) model is presented, Figure 1-a.

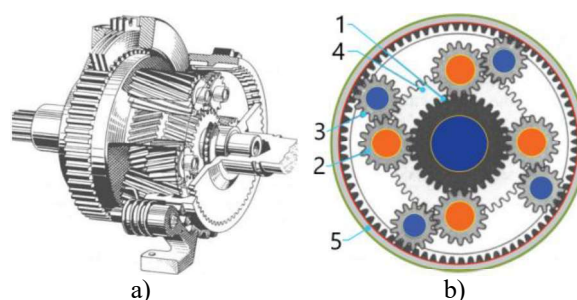


Fig. 1. Ravigneaux planetary gear train [3]

The Ravigneaux model features a compact design with a single planet carrier, three central gears (1), (4), and (5), and two planet gears (2) and (3) that are meshed with each other, Figure 1-b. By connecting the central gear (5) to the output shaft and fixing or connecting the remaining three central elements, gears (1) and (4) and the carrier to the input shaft, it is possible to achieve the max. value of six different transmission ratios. In practice, however, due to the way the aforementioned elements are connected to the components of an automatic transmission, it is possible to achieve the max. of four forward speeds and one reverse speed.

Some of the commonly used transmissions with the RPGT are: Ford AOD, ZF 4HP14, ZF 6HP19/26, Mercedes-Benz 5G-Tronic, A5S310Z for BMW 530i, Mercedes-Benz 7G-Tronic, etc.

Taking into account the complexity of the motion regarding the elements of the mentioned multi-stage RPGT, this paper will provide a systematic review of methods, emphasizing their advantages, disadvantages, and areas of applying.

## 2. Kinematic Analysis

Among the standard methods, the most widely used are Willis's equation and the general motion equation in the form of a combined method. These methods are described in detail in books [1, 2]. Using the conditions given in [1], inside [4] analytically expressed the overall transmission ratio for one of the gears of the RPGT as a function of the number of teeth of the central gears. To determine the transmission ratio, two general equations were used due to the division of the RPGT into two simple planetary gear trains.

In the following text, the methods for determining kinematics of the RPGT are presented.

### 2.1 Lever Analogy Method

Benford and Leising [5] introduced this method as a new tool for analyzing automatic transmission systems. The method is based on drawing a vertical line with corresponding points. This line represents the lever, while the points define the central elements of the RPGT. The construction of the lever for the RPGT is shown in Figure 2.

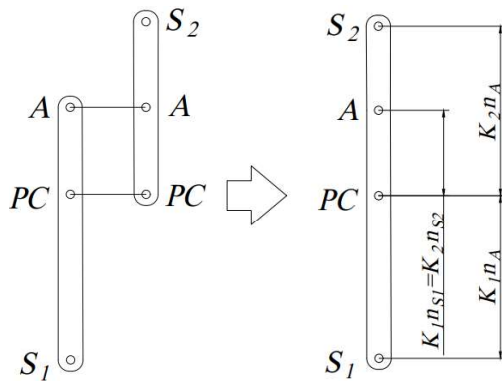


Fig. 2. Lever construction for the RPGT [8]

The RPGT represents a combination of two simple planetary gear trains in which the planet carrier (PC) and the central gear with internal teeth (A) are identical, while the central gears with external teeth (S1) and (S2) differ. By connecting their all levers, one lever for the analyzed RPGT is obtained, Figure 2.

On the obtained lever, the distances are then defined as  $K \cdot n_A$  and  $K \cdot n_S$  between the points, which represent the rotational speeds of the central gears multiplied by constants  $K_1$  and  $K_2$ . By knowing the rotational speed of the input element and fixing the corresponding gear, the scale constants can be determined based on this relationship, and using them, the rotational speeds of all elements can be calculated. Based on the obtained values of the rotational speeds for the input and output elements, the overall transmission ratio for the corresponding speed of the RPGT can be easily determined.

Today the method applying allows determining the values of loads that occur at the gear contacts. The drawback of the method is that it does not take into account data related to the planet gears and their mutual relationships. This problem was addressed in [6] by adding nodal points that define the planet gears.

### 2.2 Matrix Method Based on Graph Theory

Kinematic relationships between the elements inside RPGT can be represented with graph theory. The graph construction for the RPGT, presented in literature [7], can be seen in Figure 3-a.

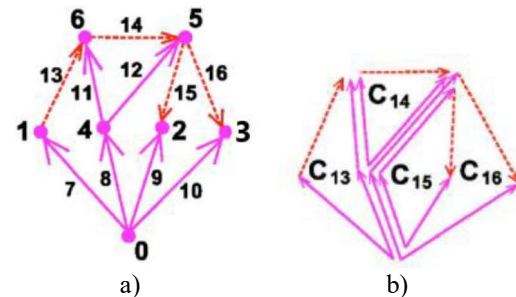


Fig. 3. Construction a)-graph and b)-of the closed loop for RPGT [7]

Node of the input shaft (0) is connected to the nodes of the central gears (1) and (2) and the planet carrier (4). The carrier node (4) is connected to the nodes of the planet gears (5) and (6). The node of the central gear with internal teeth is connected to the output shaft node, which is labeled as (0). Solid connections (7, 8, 9, 10, 11, and 12) are defined with a solid line between the nodes, while transmission connections (13, 14, 15, and 16) are represented with a dashed line. Based on its construction, closed loops can be obtained ( $C_{13}$ ), ( $C_{14}$ ), ( $C_{15}$ ) i ( $C_{16}$ ) which are shown in Figure 3-b.

For the graph in Figure 3-a, the incidence matrix is determined  $\Gamma^0 = m \times k$  ( $m$  – nodes,  $k$  – edges) the incidence matrix, which can be reduced so that the node is not included (0). Reduced matrix  $\Gamma$  can be divided into two parts from which the path matrix

is determined Z oriented graph. From this matrix, the cycle metric can be determined as the function of closed loops, Figure 3-b, and through it, the linear equation of the absolute angular speed can be obtained in the following form [7]:

$$\begin{bmatrix} -i_{13} & 0 & 0 & i_{13} + 1 & 0 & -1 \\ 0 & 0 & 0 & i_{13} + 1 & -1 & -i_{14} \\ 0 & -i_{15} & 0 & i_{13} + 1 & -1 & 0 \\ 0 & 0 & 1 & i_{13} + 1 & -i_{16} & 0 \end{bmatrix} \cdot \begin{pmatrix} \omega_1 \\ \omega_2 \\ \omega_3 \\ \omega_4 \\ \omega_5 \\ \omega_6 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}, \quad (1)$$

Where are:  $i_{13}, i_{14}, i_{15}$  i  $i_{16}$  partial transmission ratios between the elements of the RPGT, and  $\omega_i$  angular speeds of all elements. By knowing the input parameters, the matrix equation (1) is simplified. By connecting and fixing the appropriate elements of the complex PGT, the angular speeds can be expressed in matrix form  $\omega_i$ , and through them, the overall transmission ratios for each of its speeds.

The procedure for determining transmission ratios using the linear equation of absolute angular speed is presented in [8]. Unlike the previous method, this study performs a structural decomposition, where the RPGT is divided into two parts, graphically represented using a rotation graph. The rotation graph is similar to the graph in Figure 3-a. The difference is that the nodal points are connected in the form of a closed polygon. Discretization of the rotation graph into two substructures, the node matrix is determined, from which the angular speed matrix is obtained. Based on the angular speed matrix, the linear equation of angular speeds in matrix form is derived, which is similar to equation (1). The difference lies in the definition of partial transmission ratios on the left side of the equation. Solving the resulting linear equation is similar to the procedure in [7].

### 2.3 Nomogram Method

A new method for analyzing kinematic quantities, as well as torques on the elements of PGT, was developed by [9, 10], where is RPGT presented graphically using a nomogram. The construction of the nomogram involves drawing vertical lines corresponding to the angular speeds of the PGT elements relative to the horizontal axis.

In [9, 10], a detailed procedure for obtaining speeds in an automatic transmission containing the RPGT is presented. The mentioned transmission represents a conceptual design and includes two drives. The nomogram for the RPGT is shown in Figure 4. Normal (3) corresponds to the planet

carrier, the outer normals (5) and (6) to the planet gears, and normals (1), (3), and (4) to central gears.

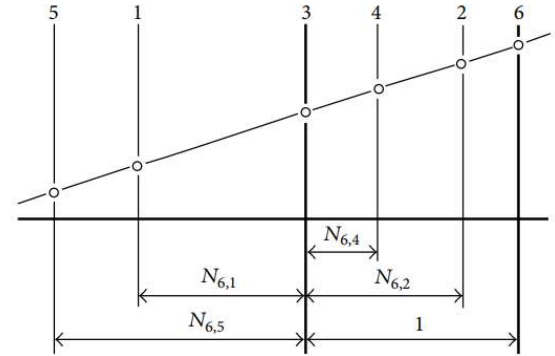


Fig. 4. Nomogram for RPGT [9]

The carrier normal (3) is placed at the zero position on the horizontal axis, and the outer planet gear (6) at a distance of 1 from normal (3), as shown in Figure 4. The distances of the other normal relative to the planet carrier normal represent the partial transmission ratios  $N_{6,1}, N_{6,2}, N_{6,4}$  i  $N_{6,5}$ . Partial transmission ratios are defined using Willis's equation:

$$N_{gb,ga} = \frac{\omega_{ga} - \omega_c}{\omega_{gb} - \omega_c} = \frac{z_{gb}}{z_{ga}}, \quad (2)$$

where are:  $\omega_{ga}, \omega_{gb}$  and  $\omega_c$  angular speeds of the input, output, and fixed elements,  $z_{gb}$  and  $z_{ga}$  the numbers of teeth of the output and input elements of the planetary gear train, respectively.

If a line is drawn at an angle across the normal, the distances of the intersected points on the normal relative to the horizontal define the angular speeds of the elements of the RPGT. Using the ratios of partial transmission on the horizontal axis and the differences in angular speeds on the vertical axis, the overall transmission ratios for each speed of the mentioned complex PGT are determined. Moreover, the advantage of the nomogram lies in drawing and determining the torque values on all elements of the RPGT, as well as listing all possible sequences of connecting the central elements with the clutches and brakes of the automatic transmission [10].

### 2.4 Discussion of Modern Methods

All three methods are based on graphical interpretation and analytical expression of transmission ratios. However, clear differences can be observed between them. The Lever Analogy Method provides precise results, provided that the distances between the nodal points on the lever are correctly defined. On the same lever, the values of peripheral speeds and torques of the elements of the RPGT can then be plotted in vector form, and their



relationships can be further analyzed in terms of dynamic analysis. The procedure is very simple, but it is not suitable for computer implementation.

According to the Lever Method, [9, 10] it is possible to graphically and analytically represent the relationships between the angular speeds of the elements inside RPGT for each gear ratio using a nomogram. On the nomogram and the lever, it is possible to plot the values of peripheral speeds and torques, which can be used for dynamic analysis. The procedure for determining the transmission ratios is more complex when using the nomogram due to the methodology required to determine the transmission ratio values for each gear. A drawback of this method is that it requires additional use of Willis's equation and is not suitable for computer implementation.

The matrix method is the most complex of the analyzed methods, as it requires knowledge of a mathematics. Although it is based on graphical interpretation, the entire procedure is analytical and time-consuming. It is suitable for computer implementation due to the use of matrices and provides the most accurate results. The method can be easily adapted to changes in the design of a complex PGT, provided that the input parameters are correctly defined. This is not the case for the other two groups of methods.

### 3. CONCLUSIONS

The analyzed methods for determining the transmission ratios, i.e., the speeds of a complex planetary gear train, are complex to execute. Unlike conventional procedures, they provide more accurate results and better insight into the relationships between the gears and the planet carrier.

By applying these methods, any complex PGT can be analyzed, provided its elements are correctly represented graphically. In addition to kinematics, the methods allow for dynamic analysis of the PGT, as well as solving the problem of connecting the central elements to the input and output shafts of the automatic transmission via clutches. This provides a better understanding of the methodology for changing speeds and the loading of the elements of the PGT.

Each method has its own advantages and disadvantages, and their practical application depends on the initial requirements set during the design of an automatic transmission.

Among the analyzed methods, the use of graphs and the incidence matrix stands out due to their accuracy, easy adaptation to changes in the PGT design, and suitability for computer implementation.

Future research will focus on applying these methods to more complex PGT with 8, 9, and 10 speeds. In addition, the conditions for proper assembly and meshing of the elements of complex PGT, which are not fully addressed by these methods, will be thoroughly investigated.

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# 41st Danubia-Adria Symposium

## Advances in Experimental Mechanics

September 23-26, 2025  
Kragujevac, Serbia

# PROCEEDINGS



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# **41<sup>ST</sup> DANUBIA-ADRIA SYMPOSIUM ADVANCES IN EXPERIMENTAL MECHANICS**

**ISBN: 978-86-6335-157-8**

**DOI: 10.46793/41DAS2025**

**Edited by:** **Miroslav Živković, Vladimir Milovanović,  
Vladimir Dunić, Aleksandar Bodić**  
Faculty of Engineering University of Kragujevac

**Publisher:** **Faculty of Engineering University of Kragujevac**

**For the publisher:** **Slobodan Savić**  
Faculty of Engineering University of Kragujevac

**Place and year of  
publication** Kragujevac, 2025

**Technical editor:** **Aleksandar Bodić, Vladimir Milovanović**  
Faculty of Engineering University of Kragujevac

**Printed by:** **Inter Print**  
Jurija Gagarina 12, 34000 Kragujevac, Serbia

**Circulation:** 100 Copies

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The publication of this Proceedings was financially supported by the Ministry of Science, Technological Development and Innovation, Republic of Serbia.



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## **PREFACE:**

Scientific conferences of Experimental Mechanics in Europe have here is a long tradition to cover all areas of experimental research in mechanics of materials and structures, including interactive fields. The first Danubia-Adria Symposium took place in 1984 in Stubicke-Toplice, Croatia, and further successfully continued in: 1985 – Graz, Austria, 1986 – Budapest, Hungary, 1987 – Plzen, Czech Republic, 1988 – Udine, Italy; 1989 – Mösern-Seefeld, Austria; 1990 – Pula, Croatia; 1991 – Gödöllő, Hungary; 1992 – Trieste, Italy; 1993 – Merin, Czech Republic; 1994 – Baden, Austria; 1995 – Sopron, Hungary; 1996 – Rajecké Teplice, Slovak Republic; 1997 – Porec, Croatia; 1998 – Bertinoro, Italy; 1999 – Cluj Napoca, Romania; 2000 – Prague, Czech Republic; 2001 – Steyr, Austria; 2002 – Polanica Zdroj, Poland; 2003 – Győr, Hungary; 2004 – Brijuni/Pula, Croatia; 2005 – Parma, Italy; 2006 – Zilina, Slovak Republic; 2007 – Sibiu, Romania; 2008 – Ceske Budejovice/Budweis, Czech Republic; 2009 – Leoben, Austria; 2010 – Wroclaw, Poland; 2011 – Siofok, Hungary; 2012 – Belgrade, Serbia; 2013 – Primosten, Croatia; 2014 – Kempten, Germany; 2015 – Stary Smokovec, High Tatras, Slovak Republic; 2016 – Portoroz, Slovenia; 2017 – Triest, Italy; 2018 – Sinaia, Romania; 2019 – Pilsen, Czech Republic; 2021 – Linz, Austria; 2022 – Poros, Greece, 2023 – Siofok, Hungary and 2024 – Gdansk, Poland.

The 41st Danubia-Adria Symposium in Kragujevac represent continuation to the series of fruitful meetings at the previous Danubia-Adria Symposia. The current Symposium DAS2025 is the second conference organized in Serbia. Serbia joint to Danubia-Adria Society on Experimental Methods in 2008 year and got active member in organization and participation of DAS which take place every year in one DA member country. This year Kragujevac has been chosen as the Conference venue and we are offering the hospitality for our Symposium. Serbian society for mechanics is the member of Danubia-Adria Society on Experimental Methods and University of Kragujevac, Faculty of Engineering is executive organizer of 41st Danubia-Adria Symposium in Advances in Experimental Mechanics.

The Faculty of Mechanical Engineering in Kragujevac, or today the Faculty of Engineering University of Kragujevac, was formed in October 1, 1960, as a department of the Faculty of Mechanical Engineering in Belgrade. The Faculty of Mechanical Engineering in Kragujevac became an independent faculty, within the University of Belgrade, on December 2, 1971. Since 1976, the Faculty of Mechanical Engineering has been part of the "Svetozar Marković" University in Kragujevac, today the University of Kragujevac.

The Faculty of Engineering University of Kragujevac is among the most reputable and prestigious scientific and educational institutions in the field of technical sciences. Today, it is a modern scientific and educational institution with a clearly defined mission, vision, goals and programmatic orientations.

The Danubia-Adria Symposium bring together internationally recognized experts and young researchers in an effort to exchange ideas on different topics of „Experimental Mechanics“. The conferences serve also a platform for establishing connections between different research teams and development of future scientific collaboration.

This year Danubia-Adria Symposium has received 57 accepted submissions from 10 countries (Austria-3, Croatia-3, Czech Republic-3, Germany-2, Hungary-7, Poland-4, Romania-3, Greece-1, Serbia-30, Bosnia & Herzegovina-1). The Program Committee selected 9 papers for keynote presentations and 48 papers for poster presentations.

We wish all participants a fruitful and enjoyable conference time in Kragujevac and hope that it will pave new ways for the development of Experimental Mechanics.

On behalf of the organizers, we would like to express our gratitude to all who showed their interest and actively helped us in preparing the event. It is a great pleasure to express our cordial thanks to all members of the Scientific Committee, to all members of the Local Organizing Committee, to all supporting institutions for their help.

Finally, on behalf of the Organizing Committee of the 41st Danubia-Adria Symposium in Advances in Experimental Mechanics, we wish a warm WELCOME to all participants in Kragujevac, and hope that all guests will have pleasant time in Serbia.


September, 2025  
Kragujevac, Serbia

Chairman of 41<sup>st</sup> DAS 2025



**Miroslav Živković**

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## TABLE OF CONTENTS:

### **KEYNOTE PRESENTATIONS:**

THE INFLUENCE OF BUILD PARAMETERS ON THE COLLAPSE BEHAVIOUR OF A HIGHLY POROUS RANDOM OPEN-CELL LATTICE 3D PRINTED IN IN718 ALLOY *Tomasz Libura, Judyta Sienkiewicz, Zbigniew Nowak, Zbigniew Kowalewski, Alexis Rusinek, George Voyiadjis, Urvashi Gunpath, Paul Wood* .....3

INFLUENCE OF STRINGER GEOMETRY ON THE STRUCTURAL INTEGRITY OF CRACKED STIFFENED PLATES *Stefan-Dan Pastrama* .....5

IMPLEMENTATION AND PRACTICAL APPLICATION OF NON-EQUIVALENT BIAXIAL MEASUREMENTS FOR HYPERELASTIC MATERIALS *Kristóf Havasi, Attila Kossa* .....7

GRP TANK LOADING INVESTIGATION USING CFS AND DFOS SENSORS *Karel Doubrava, Nikola Schmidová, David Blaha, Zdeněk Padovec, Ctirad Novotny, Radek Kottner, Radek Sedláček, Milan Růžicka* .....9

IDENTIFICATION OF ENERGETIC AND DISSIPATIVE FLOW STRESS USING INFRARED THERMOGRAPHY *Nikola Lalović, Thomas Böhlke* .....11

NOVEL TEST METHODS FOR TRIBO/MECHANICAL PROPERTIES IN THE CONTEXT OF ALTERNATIVE FUELS *Florian Grün, Peter Oberreiter, Philipp Renhart, Michael Pusterhofer* .....13

THE DEPENDENCE OF THE DEGREE OF NON-ADDITIVITY OF MECHANICALLY LOADED SYSTEMS ON THE LOADING RATE *Dimos Triantis, Ilias Stavrakas, Ermioni Pasiou, Stavros Kourkoulis* .....15

IMPACT VELOCITY INFLUENCE ON THE FRACTURE BEHAVIOUR OF PORCINE FEMURS UNDER DYNAMIC LOADING *Petra Bagavac, Marijo Bekić, Lovre Krstulović-Opara* .....17

EXPERIMENTAL ANALYSIS OF HIGH-SPEED GEARBOXES *Nenad Kolarević, Milosav Ognjanović, Miloš Stanković, Aleksandar Dimić, Nikola Davidović, Marko Miloš* .....19

### **POSTER AND ORAL PRESENTATIONS:**

EXPERIMENTAL STUDY OF HEAT EFFECT ON THE DEFORMATIONS OF AL/CU BIMETAL IN 3-POINT BENDING *Robert Uścinowicz* .....25

DYNAMIC CALIBRATION OF A MODEL OF A MIXED STRUCTURE BRIDGE DECK BASED ON DYNAMIC TESTS OF THE BRIDGE *Cristian Lucian Ghindea, Radu Iuliu Cruciat, Andrei Gheorghe Pricopie, Adrian Aurelian Diaconu, Ionut Radu Racanel* .....27

CONSTITUTIVE MODELLING OF POLYMER FOAMS USING AN ASYMMETRIC POISSON'S RATIO <i>Márton Kammerer, Attila Kossa</i> .....	29
MECHANICAL RESPONSE OF PA6 UNDER ENVIRONMENTAL CONDITIONS: A DUAL APPROACH USING EXPERIMENTS AND NUMERICAL ANALYSES <i>Nicolae Stefanoaea, Olivia-Laura Petrascu, Adrian Marius Pascu</i> .....	31
COMPARATIVE EVALUATION OF THE ELASTIC MODULUS IN CEMENT PASTES USING ULTRASONIC AND 3-MIN-CREEP TESTING <i>Sophie Schmid, Olaf Lahayne, Bernhard Pichler</i> .....	33
EXPERIMENTAL ANALYSIS OF ELECTRIC SOOTER DYNAMICS <i>Zsombor Magyari, Roland Zana, Dénes Takács</i> .....	35
EFFECTS OF STEERING ANGLE SATURATION ON STABILITY OF REVERSING TRAILERS <i>Levente Mihalyi, Denes Takacs</i> .....	37
MULTITECHNIQUE CHARACTERIZATION OF CEMENT PASTE WITH AND WITHOUT GRAPHENE OXIDE <i>Muhammad Shahid, Sophie Schmid, Olaf Lahayne, Agathe Robisson, Bernhard Pichler</i> .....	39
ANALYSIS OF TEST STRAIN IN A FOUR-POINT BENDING CALIBRATION SETUP FOR STRAIN GAGES <i>Thomas Lehmann, Tobias Jähnichen, Jörn Ihlemann</i> .....	41
STABILITY LOSS OF TAPE-SPRINGS UNDER COMPRESSIVE LOADS: A FINITE ELEMENT ANALYSIS <i>Péter Máté, András Szekrényes</i> .....	43
EXPERIMENTAL AND NUMERICAL ANALYSIS OF LASER-CUT PNEUMATIC SOFT ROBOT STRUCTURES <i>Kata Ruzsa, Szabolcs Berezvai</i> .....	45
OPTIMISING GAIT STABILITY ANALYSIS IN PATIENTS WITH MUSCULOSKELETAL DISORDERS <i>Kristóf Bányi, Zsófia Pálya, Mária Takács, Rita Kiss</i> .....	47
ALTERNATIVE METHOD OF STRESS PARAMETERS DETERMINATION DURING TENSILE TESTS USING METRIC ENTROPY AND DIC <i>Zbigniew Kowalewski, Mateusz Kopec, Grzegorz Garbacz, Adam Brodecki</i> .....	49
INFLUENCE OF TEMPERATURE ON MODE I FRACTURE TOUGHNESS OF A DUCTILE ADHESIVE <i>Lukáš Horák, Jan Krystek</i> .....	51
INVESTIGATION OF RESIDUAL STRESS EVOLUTION DUE TO CYCLIC LOADING BY YIELD SURFACE TRACKING <i>Radim Halama, Michal Kořínek, Jiří Čapek, Karel Trojan, Radim Petkov, Adam Gladiš, Jiří Hajnýš, Nikolaj Ganev</i> .....	53
DEVELOPMENT OF CONSTRUCTION FOR THE TRANSFER OF HEAVY PRISMATIC PROFILES <i>Miroslav Milutinović, Aleksandar Okilj, Sanjin Troha</i> ....	55



EXPERIMENTAL DETERMINATION OF THE EFFICIENCY OF A COMPOUND PLANETARY GEARBOX <i>Sanjin Troha, Kristina Marković, Željko Vrcan, Filip Šulj, Miroslav Milutinović</i> .....	57
EFFECT OF PRIOR CREEP ON TENSILE PROPERTIES OF AA2124/SiC COMPOSITES <i>Agnieszka Rutecka, Zbigniew Kowalewski</i> .....	59
DETERMINATION OF FOUR CHARACTERISTIC REGIONS IN THE STRESS–STRAIN RESPONSE OF APM FOAM UNDER COMPRESSION USING DVC <i>Zvonimir Tomičević, Borna Božović, Daniel Kytýř, Petr Koudelka</i> .....	61
DEVELOPMENT OF A TEST DEVICE (FIXTURE) FOR DETERMINING THE PULL-OUT FORCE OF SWAGED BALL TERMINATIONS ON CONTROL CABLES <i>Milan Blagojević, Živče Šarkočević, Milan Bojović, Ivica Čamagić</i> .....	63
QUANTITATIVE DETERMINATION OF GLASS FIBER CONTENT IN FIBER REINFORCED COMPOSITE MATERIALS <i>Milan Blagojević, Živče Šarkočević, Ivica Čamagić</i> .....	65
NUMERICAL ANALYSIS OF BARREL LOADS IN THE DESIGN PHASE OF AN ARTILLERY SYSTEM <i>Bogdan Todorović, Aleksandra Obradović, Nebojša Hristov, Damir Jerković</i> .....	67
AUTOMATION OF CONSTITUTIVE MODEL PARAMETER IDENTIFICATION <i>Dragan Rakić, Slobodan Radovanović, Miroslav Živković</i> .....	71
FATIGUE PERFORMANCE COMPARISON OF STRENGTH 700 AND 55NiCrMoV7 STEELS <i>Dušan Arsić, Gordana Jovičić, Miroslav Živković, Miloš Pešić, Marko Topalović, Đorđe Ivković, Marko Delić</i> .....	75
EXPERIMENTAL DETERMINATION OF THE EFFECT OF AXIAL FORCE ON A HEADLESS SCREW CONNECTION <i>Anđela Perović, Miloš Matejić, Vladimir Milovanović</i> .....	79
INITIAL EXPENDABLE TURBOJET PROTOTYPE TESTING EXPERIENCES <i>Nikola Davidović, Nenad Kolarević, Milos Stanković, Marko Miloš</i> .....	83
HARDNESS MEASUREMENT OF ROLLING BEARING BALLS SUBJECTED TO MULTI-CYCLE CRYOGENIC TREATMENT <i>Jovana Antić, Žarko Mišković, Danilo Pejčić, Martin Dix, Alexander Pierer, Jürgen Heidrich, Matthias Milbrandt</i> .....	87
EXPERIMENTAL AND ANALYTICAL METHODS FOR DETERMINING INTERLAMINAR SHEAR STRENGTH OF COMPOSITES MADE BY FDM 3D PRINTING <i>Nenad Grujović, Strahinja Milenković, Fatima Živić</i> .....	91
MEASUREMENT OF PIEZOELECTRIC PROPERTIES OF HYDROGELS <i>Fatima Živić, Marija Branković, Danilo Petrović, Petar Todorović, Nenad Grujović</i> .....	95

INFLUENCE OF PALLET PLACEMENT METHOD ON BEAM BEHAVIOR IN RACK STRUCTURE <i>Mirjana Piskulić, Rodoljub Vujanac, Nenad Miloradovic, Mirko Blagojevic</i> .....	99
ANALYTICAL AND FEM ASSESSMENT OF A DOUBLE-SIDED BUTT WELDED S1000QL SPECIMEN FOR TENSILE TESTING PREPARATION <i>Snežana Joksić, Jovana Živić, Marija Matejić, Miloš Matejić, Živče Šarkočević, Ivica Čamagić</i> .....	103
QUASI-STATIC TENSILE TESTING OF HIGH-STRENGTH BALLISTIC STEEL USING DIGITAL IMAGE CORRELATION – PRELIMINARY STUDY <i>Miloš Pešić, Aleksandar Bodić, Marko Topalović, Snežana Vulović, Vladimir Dunić, Vladimir Milovanović, Miroslav Živković</i> .....	107
QUASI-STATIC AND DYNAMIC BEHAVIOR OF VANADIUM-CARBIDE REINFORCED ALUMINUM ALLOY STUDIED VIA DIGITAL IMAGE CORRELATION – PRELIMINARY STUDY <i>Miloš Pešić, Aleksandar Bodić, Marko Topalović, Snežana Vulović, Vladimir Dunić, Vladimir Milovanović, Miroslav Živković</i> .....	111
EXPERIMENTAL VALIDATION OF FRICTION STIR WELDING PARAMETERS FOR EN AW 6060 T6 ALUMINUM ALLOY <i>Aleksandar Bodić, Vladimir Milovanović, Miroslav Živković, Miloš Pešić, Dušan Milojević, Marko Topalović</i> .....	115
RESIDUAL STRESS-INDUCED DAMAGE IN BRAKE DRUMS <i>Dobrivoje Čatić, Vladimir Čatić</i> .....	119
INFLUENCE OF CRACKS ON THE STRUCTURAL STABILITY OF CYLINDRICAL STEEL EQUALIZATION TANKS <i>Vladimir Milovanović, Stefan Dikić, Saša Spasenić, Mileta Ristivojević, Sreten Spasenić, Aleksandar Bodić, Miloš Pešić</i> .....	123
STRUCTURAL ASSESSMENT AND REDISIGN OF THE WATER CHAMBER IN A DOMESTIC GASIFICATION BOILER <i>Filip Nastić, Mladen Josijević, Davor Končalović, Dušan Gordić, Vladimir Vukašinović</i> .....	127
INFLUENCE OF FEED RATE ON SURFACE ROUGHNESS OF AL6088 ALLOY IN THE BALL BURNISHING PROCESS <i>Vladimir Kočović, Dragan Džunić, Sonja Kostić, Živana Jovanović Pešić, Milan Đorđević, Ljiljana Brzaković, Đorđe Vukelić</i> .....	131

EFFECT OF ELECTRON BEAM PROCESSING PARAMETERS ON THE SURFACE ROUGHNESS OF TITANIUM SAMPLES: PART II <i>Živana Jovanović Pešić, Aleksandra Vulović, Strahinja Milenković, Đorđe Ilić, Dragan Džunić</i> .....	135
2D AXISYMMETRIC VS. 3D SOLID ELEMENT PHASE-FIELD DAMAGE MODELING <i>Vladimir Dunić, Aleksandar Bodić, Miroslav Živković</i> .....	139
ANALYSIS OF DEEP DRAWING PROCESS USING FEA AND FLD <i>Marko Delić, Vesna Mandić, Srbislav Aleksandrović, Dušan Arsić, Đorđe Ivković</i> .....	143
DEVELOPMENT AND EXPERIMENTAL TESTING OF A HYDRAULIC STAND WITH PUMPS INTENDED FOR A CENTRAL HEATING SYSTEM <i>Mladen Josijević, Dušan Gordić, Davor Končalović, Filip Nastić</i> .....	147
FINITE ELEMENT ANALYSIS OF PLATELET ACTIVATION AND CELL MECHANICS IN CIRCULATING TUMOR CELL ARREST <i>Vladimir Simić, Aleksandar Nikolić, Miljan Milošević, Shao Ning, Fransisca Leonard, Miloš Kojić</i> .....	151
CONDITIONS RELATED TO THE ROOF STRUCTURE STRENGTH OF BUSES POWERED BY NATURAL GAS AND FUEL CELLS <i>Saša Milojević, Snežana Vulović, Marija Rafailović, Slobodan Savić</i> .....	155
CFD INVESTIGATION OF TURBULENT WATER FLOW IN A PIPE ELBOW: ASSESSMENT OF CAVITATION RISK <i>Payle Ljubojević, Saša Stašević</i> .....	159
KINEMATIC ANALYSIS OF THE COMPLEX PLANETARY GEAR TRAIN OVERVIEW <i>Stefan Čukic, Slavica Miladinović, Anđela Perović, Lozica Ivanović, Saša Milojević, Blaža Stojanović</i> .....	163
IMPROVEMENT OF THE TECHNICAL AND OPERATIONAL CHARACTERISTICS OF ZA-27 ALLOYS REINFORCED WITH SIC AND $Al_2O_3$ <i>Dragan Džunić, Stefan Miletić, Milan Ivković, Slobodan Mitrović</i> .....	167
CHALLENGES OF ADDITIVE MANUFACTURING IN MACHINE ELEMENT APPLICATIONS <i>Ivan Simonović, Aleksandar Marinković, Jovana Antić, Nenad Kolarević</i> .....	171
AUTHOR INDEX .....	175

CIP - Каталогизација у публикацији Народна библиотека Србије, Београд

621(082)

531(082)

**DANUBIA-Adria Symposium Advances in Experimental Mechanics (41 ; 2025  
; Kragujevac)**

Proceedings / 41st Danubia-Adria Symposium Advances in Experimental Mechanics,  
September 23-26, 2025 Kragujevac, Serbia ; edited by Miroslav Živković ... [et al.]. -  
Kragujevac : University, Faculty of Engineering, 2025 (Kragujevac : Inter Print). - [16],  
177 str. : ilustr. ; 30 cm

Tiraž 100. - Str. [9-10]: Preface / Miroslav Živković, Vladimir P. Milovanović. -  
Bibliografija

uz svaki rad. - Registar.

ISBN 978-86-6335-157-8

1. Živković, Miroslav, 1962- [urednik] [autor dodatnog teksta] 2. Milovanović, Vladimir,  
1979- [urednik] [autor dodatnog teksta] 3. Dunić, Vladimir, 1983- [urednik] 4. Bodić,  
Aleksandar S., 1997- [urednik]

a) Механика -- Зборници b) Технички материјали -- Испитивање -- Зборници

COBISS.SR-ID 175480073



